

EE 193 - Applied Probability and Statistics for Engineers
Department of Electrical and Computer Engineering
Tufts University Fall 2007

Problem Set #1 Distributed September 7, 2007
Due Sept. 20, 2007

Problem 1

Poor old Prof. Mash may have had a bit too much to drink at the latest faculty meeting and has been pulled over by the local constabulary after a bit of erratic driving. To ascertain just how much of a danger the good professor is to the public, he is asked to walk a straight line. Being somewhat compulsive, Mash takes one step forward (exactly 1 m) each and every second. Unfortunately, he is also somewhat, shall we say, wobbly, and with each step forward there is a chance he also moves to the right or to the left. Specifically, with probability $1/3$ he moves 1 m to the left with each step, with probability $1/3$ he goes to the right, and with probability $1/3$ he only moves forward (i.e., no sideways wobble). More formally, let x be the axis along which Prof. Mash is *supposed* to be walking and y the perpendicular direction of wobble.

- (a) What is the sample space for this problem in the case where the professor is allowed to take an infinite number of steps.
- (b) Find the probability law for the location of the professor after three seconds.
- (c) What is the probability that after 10 seconds Prof. Mash is located at $x = 10\text{m}$ and $y = 0\text{m}$.
- (d) Prof. Mash will be thrown in the slammer if he deviates by at most 1 m to the right or to the left at any point along his walk. Let n be the number of seconds the police allow Mash to walk. What is the probability as a function n that poor Prof. Mash is going to need to call the local bail bondsman?

Problem 2

Yates and Goodman problems

- 1.2.1 (a)–(c)
- 1.3.2
- 1.4.1
- 1.4.4 parts (a) and (c)
- 1.4.7
- 1.5.5
- 1.11.2