Warmup

 Write the following binary numbers in decimal:

 8
 4
 1
 32
 6
 4
 16

 100
 101010
 1111
 1111
 1111

 12
 32
 8
 4
 2
 1111
 1111

 12
 32
 8
 4
 2
 1111
 1111

 12
 32
 8
 4
 2
 1111
 1111

Submit your answer on pollev.com/stevenbell

ES 4: Number systems (and more VHDL) (sorry)

Steven Bell 28 September 2023



What's the point?

Any useful computer will need to deal with negative numbers

If you know how negative numbers are represented: a) You can explain why the computer gets "interesting" results b) You can build a circuit that operates on negative numbers (like a computer!)

By the end of class today, you should be able to:

- Convert between hexadecimal and binary
- Convert between 2's complement binary and decimal
- Explain why we prefer 2's complement to sign-magnitude
- Explain the VHDL types: bit, std_logic, integer, unsigned, signed.

Hexadecimal

Is just a shorthand for binary numbers, because no one can read 0001011110010101

0000 0001 left-pad with 0 as needed! 1000

C

g

Practice!

Write the following binary numbers in hex:

Write these hexadecimal numbers in binary:

 FF
 80
 DEAD

 111111
 101110
 1010

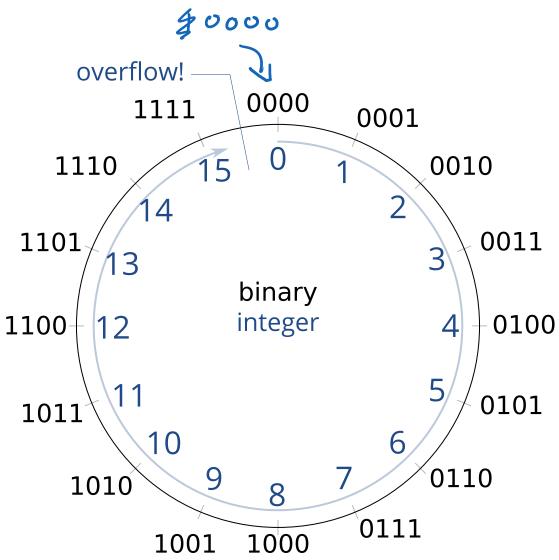
 1000000

Submit binary \rightarrow hex answers on **pollev.com/stevenbell**

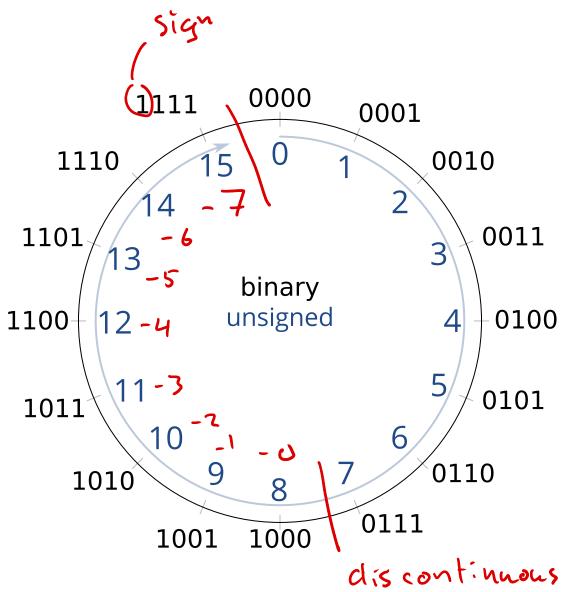
There are 10 kinds of people in the world. Those who understand binary, and those who don't.

There are $\frac{10}{8}$ kinds of people in the world. Those who understand hexadecimal, and those who don't.

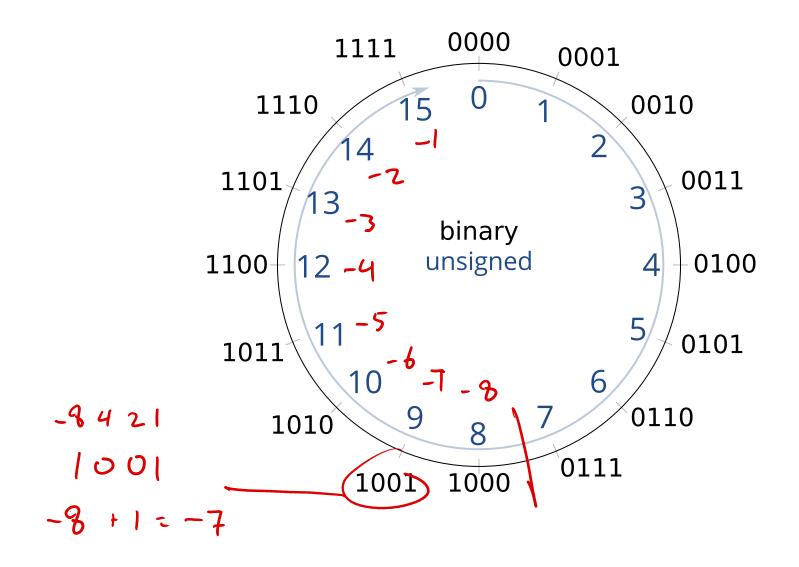
Unsigned numbers

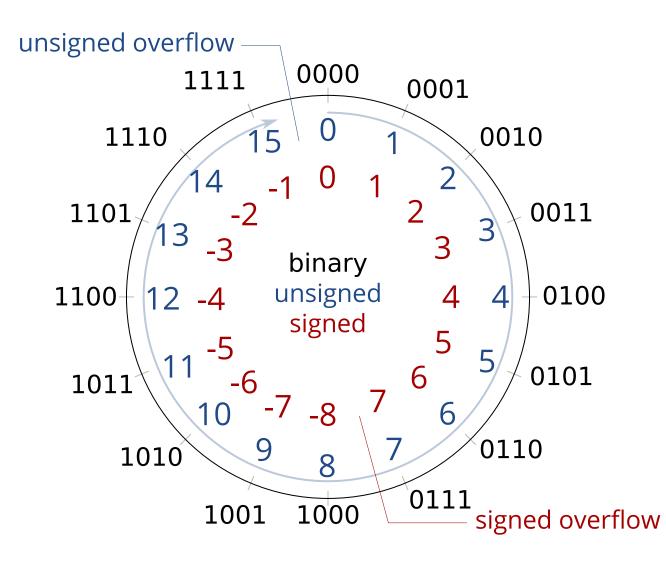


Sign-magnitude



Two's complement





To write a negative number in 2's complement:

Write the positive number in binary Flip all the bits $(1 \rightarrow 0, 0 \rightarrow 1)$

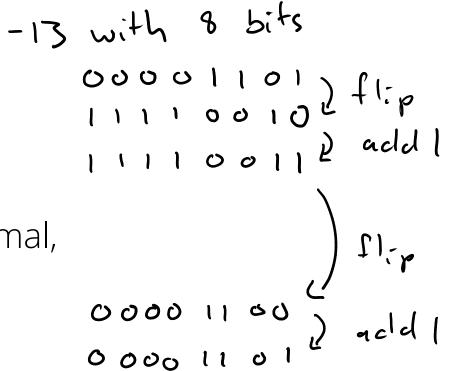
Add 1 (with all the appropriate carries)

To convert negative 2's complement to decimal,

Flip all the bits $(1 \rightarrow 0, 0 \rightarrow 1)$

Add 1 (with all the appropriate carries)

Write the number in decimal



Wait, shouldn't this be reversed? It turns out the result is the same either way. Try it!

Practice!

Write the following numbers in 8-bit 2's complement:

Find the decimal value of these 2's complement numbers: 8421 , 1111110, 10000000 decimal

Submit your decimal answers on **pollev.com/stevenbell**

What's the point?

Practically all real systems use 2's complement

So why did we waste all that time with sign-magnitude? Because sign-magnitude seems "obvious" and 2's complement is "weird"

Floating-point numbers do use sign-magnitude

8 to 16 - bit:

... 000 0000 0101 5

Numbers in VHDL

Types

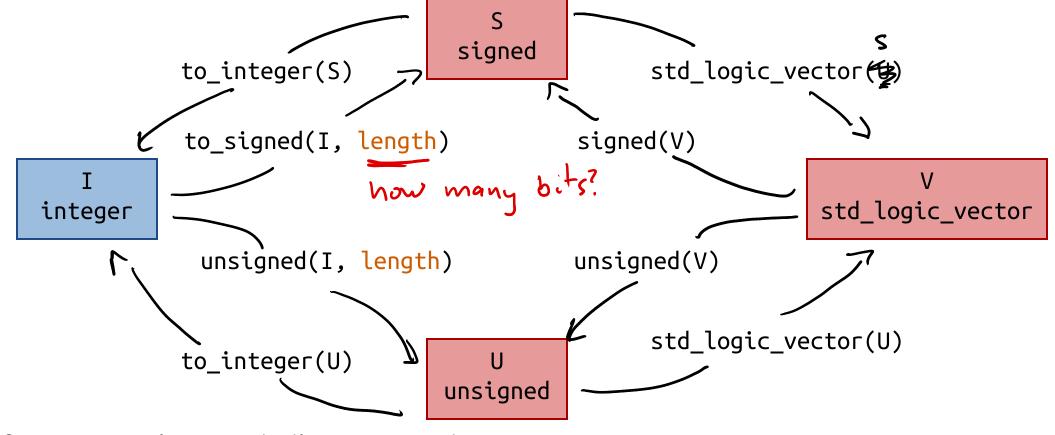
std_logic Basic logic type, can take values 0, 1, X, Z (and others)
std_logic_vector (n downto m) Ordered group of std_logic
unsigned (n downto m) Like std_logic_vector, but preferred
signed (n downto m) for numerically meaningful signals
integer Poor for synthesis, but constants are integers by default

Literals '0', '1', 'X', 'Z' "00001010", x"0c" 8-bit binary, hex 9x"101" 3b"101" 7d"101" 9-bit hex 3-bit binary 7-bit decimal 5, 38, 10000000

Converting numeric types Numbers Not good for synthesis!

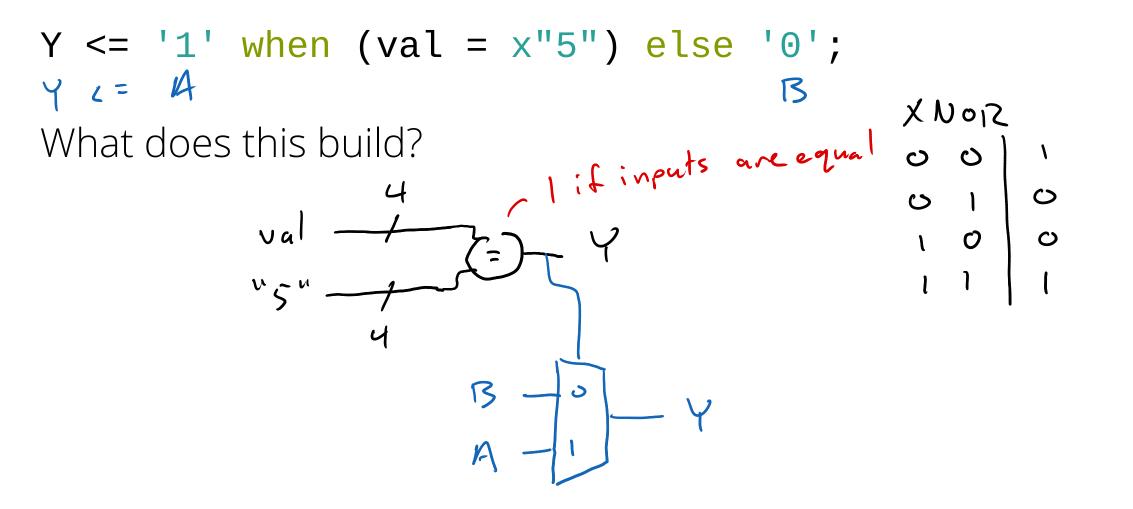


Have a defined bit representation (length + ordering)



https://fpgatutorial.com/vhdl-types-and-conversions/

When/else



Practice!

Multiplexer, thermometer decoder, 4-bit ALU

For next time

- 1. Read the book (4.3, 4.9) and complete the pre-class quiz
- 2. Lab report 2 due this week
- 3. Lab report 3 due in 2 weeks
- 4. No prelab for lab 4 (yay!)